CSCI 340 — Homework 2

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Due: February 5, 2021 @ 11:59PM

- 1. For each of the problems below, give a regular expression which only accepts the following. Assume $\Sigma = \{a \ b\}$
 - (a) All strings that begin and end with the same letter
 - (b) All strings in which the total number of *a*'s is divisible by 3
 - (c) All strings that end in a double letter
- 2. Show the following pairs of regular expressions define the same language
 - (a) $(\mathbf{ab})^*\mathbf{a}$ and $\mathbf{a}(\mathbf{ba})^*$
 - (b) $(\mathbf{a}^*\mathbf{b}\mathbf{b}\mathbf{b})^*\mathbf{a}^*$ and $\mathbf{a}^*(\mathbf{b}\mathbf{b}\mathbf{b}\mathbf{a}^*)^*$
- 3. Describe (in English phrases) the languages associated with the following regular expressions
 - (a) $(\mathbf{a} + \mathbf{b})^* \mathbf{a} (\lambda + \mathbf{b} \mathbf{b} \mathbf{b} \mathbf{b})$
 - (b) $(\mathbf{a}(\mathbf{a}\mathbf{a})^*\mathbf{b}(\mathbf{b}\mathbf{b})^*)^*$
 - (c) $((\mathbf{a} + \mathbf{b})\mathbf{a})^*$
- 4. Build an FA that accepts only the language of all words with b as the second letter. Show both the picture and the transition table for this machine and find a regular expression for the language.
- 5. Find two FA's that satisfy these conditions: Between them they accept all words in $(a + b)^*$, but there is no word accepted by both machines.
- 6. Describe the languages accepted by the following FA's:
 - (a)



(b)

