


Outline

- Semantics
- Attribute Grammars
- Categories of Semantics
 - Operational
 - Denotational
 - Axiomatic

Semantics

- the *meaning* of the expressions, statements, and program units
- Why care? So we...
 - Know how a language works
 - Understand what various statements mean
 - Improve our ability to learn a new language quickly



Attribute Grammars

Attribute Grammars

- Addition to the **syntactic** grammar of a language
- Describes a small subset of **semantic** behavior
- Why care?
 - Static semantics specification
 - Compiler design (static semantics checking)

Attribute Grammars

- Each grammar **symbol** has:
 - A set of attribute values **A**
- Each grammar **rule** has:
 - a set of functions **F** that define certain attributes of the nonterminals in the rule
 - a (possibly empty) set of predicates **P** to check for attribute consistency

Remember, a Grammar already has:

Start, Nonterminals, Terminals, Rules

Attribute Grammars

Rules have the form:

$$X_0 \rightarrow X_1 \dots X_n$$

We also have:

- **Synthesized Attributes** – a.k.a. information which is realized during the parsing (bottom – up)
- **Inherited Attributes** – a.k.a. information which is defined based on the structure (top – down)
- **Intrinsic Attributes** – a.k.a. static information affixed to Leaves/Terminals

Example Attribute Grammar

- Syntax

$\langle \text{assign} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{expr} \rangle \rightarrow \langle \text{var} \rangle + \langle \text{var} \rangle \mid \langle \text{var} \rangle$

$\langle \text{var} \rangle \rightarrow A \mid B \mid C$

- Attributes:

- **actual_type**: synthesized for $\langle \text{var} \rangle$ and $\langle \text{expr} \rangle$

- **expected_type**: inherited for $\langle \text{expr} \rangle$

Example Attribute Grammar

- Syntax Rule:

$\langle \text{expr} \rangle \rightarrow \langle \text{var} \rangle[1] + \langle \text{var} \rangle[2]$

- Semantic Rules:

$\langle \text{expr} \rangle.\text{actual_type} \leftarrow \langle \text{var} \rangle[1].\text{actual_type}$

- Predicates:

$\langle \text{var} \rangle[1].\text{actual_type} == \langle \text{var} \rangle[2].\text{actual_type}$

$\langle \text{expr} \rangle.\text{expected_type} == \langle \text{expr} \rangle.\text{actual_type}$

Example Attribute Grammar

- Syntax Rule:

`<var> → id`

- Semantic Rules:

`<var>.actual_type ← lookup(id.string)`

- Predicates:

None

Example Attribute Grammar

- Syntax Rule:

`<assign> → <var> = <expr>`

- Semantic Rules:

`<expr>.expected_type ← <var>.actual_type`

- Predicates:

`<var>.actual_type == <expr>.actual_type`

How are Attribute Values Computed?

- If all attributes were **inherited**, the tree could be decorated in top-down order
- If all attributes were **synthesized**, the tree could be decorated in bottom-up order
- In most cases, both kinds of attributes are used, so we use some combination of top-down and bottom-up

Example

Suppose we have the following code:

```
z = x + y
```

Type Information:

- `x` is an `int`
- `y` is an `int`
- `z` is a `string`

Example

$z = x + y$

`<assign>`
actual=
expected=

`<var>` =
actual=

id
string=z

`<var>[1]` + `<var>[2]`
actual= actual=

id
string=x

id
string=y

`<expr>` \rightarrow `<var>[1]` + `<var>[2]`
`<expr>.actual_type` \leftarrow `<var>[1].actual_type`

Predicates:

`<var>[1].actual_type` == `<var>[2].actual_type`
`<expr>.expected_type` == `<expr>.actual_type`

`<var>` \rightarrow id
`<var>.actual_type` \leftarrow lookup(id.string)

Predicates:

None

`<assign>` \rightarrow `<var>` = `<expr>`
`<expr>.expected_type` \leftarrow `<var>.actual_type`

Predicates:

`<var>.actual_type` == `<expr>.actual_type`

Example

$x = x + y$

`<assign>`
actual=
expected=

`<var>` =
actual=

id
string=x

`<var>[1]` + `<var>[2]`
actual= actual=

id
string=x

id
string=y

`<expr>` \rightarrow `<var>[1]` + `<var>[2]`
`<expr>.actual_type` \leftarrow `<var>[1].actual_type`

Predicates:

`<var>[1].actual_type` == `<var>[2].actual_type`
`<expr>.expected_type` == `<expr>.actual_type`

`<var>` \rightarrow id

`<var>.actual_type` \leftarrow lookup(id.string)

Predicates:

None

`<assign>` \rightarrow `<var>` = `<expr>`

`<expr>.expected_type` \leftarrow `<var>.actual_type`

Predicates:

`<var>.actual_type` == `<expr>.actual_type`



Categories of Semantics

Operational Semantics

- Describe the meaning of a program by executing its statements on a machine
 - The machine can be either simulated or actual
 - The change in the state of the machine (memory, registers, etc.) defines the meaning of the statement
- *To use operational semantics for a high-level language, a virtual machine is needed*

Operational Semantics

- Uses of operational semantics:
 - Language manuals and textbooks
 - Teaching programming languages
- Evaluation
 - Good if used informally (language manuals, etc.)
 - Extremely complex if used formally

Denotational Semantics

- Based on recursive function theory
- The most abstract semantics description method
- The process of building a denotational specification for a language:
 1. Define a mathematical object for each language entity
 2. Define a function that maps instances of the language entities onto instances of the corresponding mathematical objects
- The meaning of language constructs are defined by only the values of the program's variables

Denotational Semantics

$\langle \text{digit} \rangle \rightarrow '0' \mid '1' \mid '2' \mid '3' \mid '4'$
 $\quad \quad \quad \mid '5' \mid '6' \mid '7' \mid '8' \mid '9'$

$\langle \text{dec_num} \rangle \rightarrow \langle \text{digit} \rangle \mid \langle \text{dec_num} \rangle \langle \text{digit} \rangle$

$$M_{\text{dec}}('0') = 0$$

$$M_{\text{dec}}('1') = 1$$

...

$$M_{\text{dec}}('9') = 9$$

$$M_{\text{dec}}(\langle \text{dec_num} \rangle '0') = 10 * M_{\text{dec}}(\langle \text{dec_num} \rangle)$$

$$M_{\text{dec}}(\langle \text{dec_num} \rangle '1') = 10 * M_{\text{dec}}(\langle \text{dec_num} \rangle) + 1$$

...

$$M_{\text{dec}}(\langle \text{dec_num} \rangle '9') = 10 * M_{\text{dec}}(\langle \text{dec_num} \rangle) + 9$$

Operational vs. Denotational

- In **operational semantics**, the state changes are defined by coded algorithms
- In **denotational semantics**, the state changes are defined by rigorous mathematical functions
 - We only looked at defining a number
 - Imagine an entire program/loop!

Axiomatic Semantics

- Based on **formal logic** (predicate calculus)
- Original purpose
 - Formal Program Verification
- Axioms are defined for each statement type in the language
 - to allow transformations of logic expressions into more formal logic expressions
 - Also known as inference rules
- The logic expressions are called **assertions**