## CSCI 340 - Homework 2

## Professor Killian

Due: February 3, 2019 @ 11:59PM

1. For each of the problems below, give a regular expression which only accepts the following. Assume $\Sigma=\left\{\begin{array}{ll}a & b\end{array}\right\}$
(a) All strings that begin and end with the same letter
(b) All strings in which the total number of $a$ 's is divisible by 3
(c) All strings that end in a double letter
2. Show the following pairs of regular expressions define the same language
(a) (ab)* and $\mathbf{a}(\mathbf{b a})^{*}$
(b) ( $\left.\mathbf{a}^{*} \mathbf{b b b}\right)^{*} \mathbf{a}^{*}$ and $\mathbf{a}^{*}\left(\mathbf{b b b a}^{*}\right)^{*}$
3. Describe (in English phrases) the languages associated with the following regular expressions
(a) $(\mathbf{a}+\mathrm{b})^{*} \mathrm{a}(\lambda+\mathrm{bbbb})$
(b) $\left(\mathbf{a}(\mathrm{aa})^{*} \mathbf{b}(\mathrm{bb})^{*}\right)^{*}$
(c) $((a+b) a)^{*}$
4. Build an FA that accepts only the language of all words with $b$ as the second letter. Show both the picture and the transition table for this machine and find a regular expression for the language.
5. Find two FA's that satisfy these conditions: Between them they accept all words in $(\mathbf{a}+\mathbf{b})^{*}$, but there is no word accepted by both machines.
6. Describe the languages accepted by the following FA's:
(a)

(b)

(c)

